

# MAASAI MARA UNIVERSITY 

# REGULAR UNIVERSITY EXAMINATIONS 

 2018/2019 ACADEMIC YEAR FIRST YEAR FIRSTSEMESTER
# SCHOOL OF BUSINESS AND ECONOMICS BSC. ECONOMICS/BSC. FINANCIAL ECONOMICS/BSC. ECONOMICS AND STATISTICS BACHELOR OF SCIENCE IN ECONOMICS 

## COURSE CODE: ECO 1104 COURSE TITLE:FUNDAMENTALS OF MATHEMATICS

INSTRUCTIONS TO CANDIDATES
Answer ALL questions in SECTION A and ANY OTHER THREE questions from SECTION B

## SECTION A (25 MARKS)

## Question one (25Marks)

a) State two broad applications of mathematics in economic analysis (2 Marks)
b) A new car has been bought for $\$ 75000$ and is assumed to decrease in value by $5 \%$ per year over aten -year period. What is its value after tenyears?(3 Marks)
c) Give economic interpretations to each of the following expressions and then use a calculator to find the appropriate values
i. $50000(1.07)^{14}$ (3 Marks)
ii. $7500(0.86)^{20}$ (3 Marks)
d) A ball with radius $r$ metres has a volume of $\frac{4}{3} \pi r^{3}$ cubic metres. By how much does the volume expand if the radius increases by one metre.
(3 Marks)
e) Find what values of $x$ satisfy $10 x-6 \geq x+12$ (3Marks)
f) At the beginning of the year, an investor had $£ 50000$ in two bank accounts, each of which paid interest annually. The interest rates were $4 \%$ and $6 \%$ per annum respectively. If the investor has made no withdrawals during the year and has earned a total of has made no withdrawals during the year and has earned a total of $£ 2750$ interest, what was the initial balance in each of the two accounts?
(4 Marks)F
g) Solve the systems of equations

> i. $2 x-6 y=4$ $x-8 y=2$ (2Marks)
> ii. $2 x-4 y=19$
> $-5 x+3 y=11$ (2Marks)

## SECTION B (45 MARKS)

## Question two (15Marks)

a) Sketch a graph of the straight line $y=2 x+3$ for $0 \leq x \leq 4$ (2 Marks)
b) Determine the slope and intercept of the straight line $9 x+3 y=4$ ( $\mathbf{3}$ Marks)
c) A person has $£ 120$ to spend on two goods ( $X, Y$ ) whose respective prices are $£ 3$ and $£ 5$.
i. Draw a budget line showing all the different combination of the two goods that can be bought with the given budget B.(4 Marks)
ii. What happens to the original budget line if the budget falls by $25 \%$ ? Hence draw the budget line on the same graph in (i) above. (3 Marks)
iii. What happens to the original budget line if the price of X doubles? Hence draw the budget line on the same graph in (i) above. (3 Marks)

## Question three (15Marks)

a) The demand and supply equation of a good are given by

$$
4 P=-Q_{d}+240
$$

$5 P=Q_{s}+30$ Determine the equilibrium price and quantity.(3 Marks)
b) The demand and supply functions of a good are given by

$$
P=-Q_{d}+125
$$

$2 P=3 Q_{s}+30$ Determine:
i. The equilibrium price and quantity
(2Marks)
ii. The effect on the market equilibrium if the government decides to impose a fixed tax of $£ 5$ on each good.
(3Marks)
iii. Who pays the tax? Hence or otherwise how much? (2 Marks)
c) Sketch the graph of the function $f(x)=2 x^{2}+3 x-2$ for integer values of $x$ for which $-4 \leq x \leq 2$. Hence solve the equation $2 x^{2}+3 x-2=0$ using the graph. (5 Marks)

## Question four (15Marks)

a) Solve the quadratic equation $4 x^{2}-11 x+6=0$ using the formula.(3Marks)
b) If the fixed costs are 18 , variable costs per unit are 4 and the demand function is $P=24-2 Q$.
i. Obtain an expression for profit function, $\pi$ in terms of $Q$. Hence or otherwise sketch a graph of $\pi$ against Q for $P=24-2 Q$.( $\mathbf{8}$ Marks)
ii. For what values of Q does the firm break even?
iii. Determine the maximum value of the profit function.
(1Marks)
(3 Marks)

## Question five (15 Marks)

a) Simplify the expression
i. $\frac{Y-1}{Y+1}-\frac{1-Y}{Y-1}-\frac{-1+4 Y}{2(Y+1)}$ ( $\mathbf{3}$ Marks)
ii. $\frac{X-Y}{X+Y}-\frac{X}{X-Y}+\frac{3 X Y}{X^{2}-Y^{2}}$ (4 Marks)
b) Let $A=\{11,12,13,14,15\}$ and $B=\{13,16\}$. Find: -
i. $A \cup B$ (1 Mark)
ii. $A \cap B$ (1 Mark)
iii. $A \backslash B$
(1 Mark)
iv. $B \backslash A$
(1 Mark)
c) An electrical company has a budget of $£ 6000$ a week to spend on the manufacture of toasters and kettles. It costs $£ 5$ to manufacture a toaster and $£ 12$ to manufacture a kettle. Write down the equation of the budget line and sketch its graph.

