## MAASAI MARA UNIVERSITY

# REGULAR UNIVERSITY EXAMINATIONS 2023/ 2024 ACADEMIC YEAR 

THIRD YEAR FIRST SEMESTER SCHOOL OF BUSINESS AND ECONOMICS. DEGREE IN BACHELOR OF ECONOMICS.

## COURSE CODE: ECO 3107-1 COURSE TITLE: OPERATIONS RESEARCH.

## INSTRUCTIONS TO CANDIDATES

Answer Question ONE and any other TWO questions

## QUESTION ONE

a. Give two differences between graphical and algebraic methods of solving linear programming problems
(4 marks)
b. Explain what is meant by optimality condition and feasibility condition
(4 marks)
c. PERT/CPM networks consists of two major components, discuss
(4marks)
d. Kenya airlines uses 650 taillights in every year. Each time an order for taillights is placed, an ordering cost of 450 shillings is incurred. Each light cost 50 shillings and holding cost is 10 shillings per light per year. Assume that demand occur at constant rate and shortages are not allowed. What is EOQ and how many time will elapse between the placement of orders?
(4 marks)
e. Consider the following linear programming, provide the algebraic solution for the model.
Maximize $z=2 x_{1}+3 x_{2}$
Subject to: $2 x_{1}+x_{2} \leq 4$
$x_{1}+2 x_{2} \leq 5$
$x_{1}, x_{2} \geq 0$
(4 marks)

## QUESTION TWO

a. In a departmental store one cashier is there to serve the customers. And the customers pick up their need by themselves. The arrival rate is 8 customers for every 4 minutes and the cashier can serve 10 customers in 4 minutes. Assuming Poisson arrival rate and exponential distribution for service rate, find:
i. Average number of customers in the system
ii. Average queue length
iii. Average time a customer spend in the queue
iv. Average time a customer spend in the system
(2 marks)
b. A departmenthead has four subordinates, and four tasks to be performed. The subordinates differ in efficiency, and the tasks differ in their intrinsic difficultly. His estimate of the time each person would take to perform each task is given in the table. How should the tasks be allocated, one to a person, so as to minimize the total man-hours?

| TASKS | MAN |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | I | II | III | IV |  |
|  | A | 8 | 26 | 17 | 11 |  |
|  | B | 13 | 28 | 4 | 26 |  |
|  | C | 38 | 19 | 18 | 15 |  |
|  | D | 19 | 26 | 24 | 10 |  |

(7 marks)

## QUESTION THREE

a. Kericho tea company produces tea for local use, internal market and external/export from three tea plant species, T1, T2and T3, as provided in the following table.

| Tea plant | Tons of tea |  | Maximum |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Local <br> use | Internal <br> use | External <br> use <br> daily <br> available <br> tons |  |
| T1 | 1 | 2 | 1 | 430 |
| T2 | 3 | 0 | 2 | 460 |
| T3 | 1 | 4 | 0 | 420 |
| Profit per ton <br> (Ksh.1000) | 3 | 2 | 5 |  |

Kericho tea company wants to determine the optimum (best) product mix for local, internal and external market that maximizes the daily profit. Find an optimal solution to this problem using the simplex technique.
(15 marks)

## QUESTION FOUR

a. The costs in dollars of driving a truck between cities as well as the surplus and shortage values of each metropolitan area is provided in the following table. Find the optimum solution using Vogels method
(7 marks)

| Origin (surplus <br> area) | Destination (shortage area) |  |  | Supply (surplus of <br> trucks) |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 110 |  |
| 2 | 50 | 100 | 100 |  |  |
| 3 | 200 | 300 | 200 |  |  |
| Demand <br> (shortage) | 140 | 200 | 80 | 160 |  |

b. Bata shoe company produces shoes for internal and external markets from two raw materials, R1 and R2. The following table provide the data.

|  | Tons of raw materials |  |  |
| :---: | :---: | :---: | :---: |
|  | Internal market | External <br> market | Maximum daily <br> available (tons) |
| R1 | 5 | 4 | 22 |
| R2 | 1 | 2 | 7 |
| Profit per ton | 6 | 4 |  |

Determine the optimum distribution for internal and external markets that maximizes the daily profits using algebraic method

